

Fourth Semester B.E. Degree Examination, June-July 2009
Field Theory

Time: 3 hrs.

Max. Marks:100

**Note: Answer any FIVE full questions, selecting
at least TWO questions from each part.**

PART - A

- 1 a. State and explain experimental law of Coulomb. (05 Marks)
- b. Identical point charges of $3\mu\text{C}$ are located at the four corners of the square of 5cm side, find the magnitude of force on any one charge. (08 Marks)
- c. Using Gauss law, determine electric field intensity every where due to a hollow sphere of charge. (07 Marks)

- 2 a. Obtain an expression for the energy expanded in moving a point charge in an electric field. (05 Marks)
- b. Potential is given by $V = 2(x+1)^2(y+2)^2(z+3)^2$ volts in free space. At a point P(2, -1, 4) calculate i) Potential ii) Electric field intensity iii) Flux density and iv) Volume charge density. (08 Marks)
- c. Obtain boundary conditions for dielectric-dielectric boundary. (07 Marks)

- 3 a. Explain Poisson's equation & Laplace equation. (05 Marks)
- b. Given the potential field $V = [Ar^4 + Br^{-4}] \sin 4\phi$ volts. Show that $\nabla^2 V = 0$, select A & B so that $v = 100$ volts and $|\vec{E}| = 500$ v/m at P($r = 1, \phi = 22.5^\circ, z = 2$). (08 Marks)
- c. State and prove Uniqueness theorem. (07 Marks)

- 4 a. Using Biot Savart's law, obtain magnetic field intensity expression due to an infinite length conductor carrying current I. (05 Marks)
- b. Derive the general expression for the field \vec{B} at any point along the axis of a solenoid. (08 Marks)
- c. Define vector magnetic potential. Prove that $A = \int \frac{\mu_0 J dv}{4\pi R}$. (07 Marks)

PART - B

- 5 a. Derive Lorentz force equation and mention the application of the solution. (05 Marks)
- b. Derive an expression for the force on a differential current element placed in a magnetic field. Find the force per meter length between two long parallel wires separated by 10cm in air and carrying a current of 10A in the same direction. (08 Marks)
- c. Derive differential form of continuity equation. (07 Marks)

- 6 a. What is the inconsistency of Ampere's law with the equation of continuity? Derive the modified form of Ampere's law of Maxwell. (05 Marks)
- b. Given $\vec{E} = E_0 \sin(\omega t - \beta z) \hat{a}_y$ v/m in free space. Find i) \vec{D} ii) \vec{B} iii) \vec{H} . Sketch \vec{E} & \vec{H} at $t = 0$. (08 Marks)
- c. Write Maxwell's equation in point form and in integral form for time varying fields. (07 Marks)

- 7 a. Define wave equation. Derive the wave equation for \vec{E} in a general medium. (05 Marks)
- b. For an electromagnetic wave propagating in free space, prove that
- i) $\frac{|\vec{E}|}{|\vec{H}|} = \eta$ ii) \vec{E} & \vec{H} are mutually perpendicular (08 Marks)
- c. State and prove Poynting theorem. (07 Marks)
- 8 a. Define 'depth' of penetration'. Show that depth of penetration of a wave in a conductor decreases with an increase in frequency. (05 Marks)
- b. Show that at any instant the magnetic and electric field in a reflected wave are out-of phase by 90° . (08 Marks)
- c. Define Brewster's angle. Derive the necessary expression in terms of permittivity. (07 Marks)